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ARTHUR CAYLEY, S.D., F.R.S.  
MATHEMATICAL PAPERS.



THE COLLECTED  
MATHEMATICAL PAPERS

OF

ARTHUR CAYLEY, Sc.D., F.R.S.,

SADLERIAN PROFESSOR OF PURE MATHEMATICS IN THE UNIVERSITY OF CAMBRIDGE.

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