Developments in Fuzzy Sets,
Intuitionistic Fuzzy Sets,
Generalized Nets and Related Topics.
Volume I: Foundations

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## Systems Research Institute Polish Academy of Sciences

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Krassimir T. Atanassov Michał Baczyński Józef Drewniak Janusz Kacprzyk Maciej Krawczak Eulalia Szmidt Maciej Wygralak Sławomir Zadrożny



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### Contents

Foreword	V
Intuitionistic fuzzy subtractions - $^{\prime \epsilon, \eta}$ and $- ^{\prime \prime \epsilon, \eta}$	1
Stability conditions for generalized nets  K. T. Atanassov, I. M. Stamova and V. K. Atanassova	. 11
On intuitionistic fuzzy multi-dimensional sets. Part 3  K. T. Atanassov, E. Szmidt and J. Kacprzyk	. 19
On intuitionistic fuzzy subtractions $-\frac{1}{19}$ and $-\frac{11}{19}$ L. Atanassova	. 27
S-implications in Atanassov's intuitionistic and interval-valued fuzzy set theory revisited	. 33
A Jensen type inequality for Sugeno integrals with respect to intuitionistic fuzzy measures	. 43
Generalized inverses for monotonic operations. A survey	. 53
Connection between balanced fuzzy set and Atanassov intuitionistic fuzzy setP. Drygaś	. 63
Hudetz entropy on IF-events	. 73

Product of intuitionistic fuzzy groups	87
Knowledge from contradiction and inconsistency  C. J. Hinde	95
Estimation of the relations: preference, equivalence and tolerance on the basis of pairwise comparisons	09
On Fuzzy implications with ordered fuzzy numbers	21
The individual ergodic theorem on IF events	31
Eigen fuzzy vectors for min- * product	41
Properties of interval-valued fuzzy relations and Atanassov operators 1  B. Pękala	53
On the probability theory on the Kôpka D-posets	67
On intuitionistic fuzzy trees	77
Representing intuitionistic fuzzy sets as metasets	85
On the Hamming-metric-based Hausdorff distance for intuitionistic fuzzy sets and interval-valued fuzzy sets	09

The papers presented in this Volume 1 constitute a collection of contributions, both of a foundational and applied type, by both well-known experts and young researchers in various fields of broadly perceived intelligent systems.

It may be viewed as a result of fruitful discussions held during the Eighth International Workshop on Intuitionistic Fuzzy Sets and Generalized Nets (IWIFSGN-2009) organized in Warsaw on October 16, 2009 by the Systems Research Institute, Polish Academy of Sciences, in Warsaw, Poland, Centre for Biomedical Engineering, Bulgarian Academy of Sciences in Sofia, Bulgaria, and WIT – Warsaw School of Information Technology in Warsaw, Poland, and co-organized by: the Matej Bel University, Banska Bistrica, Slovakia, Universidad Publica de Navarra, Pamplona, Spain, Universidade de Tras-Os-Montes e Alto Douro, Vila Real, Portugal, and the University of Westminster, Harrow, UK:

http://www.ibspan.waw.pl/ifs2009

The Eighth International Workshop on Intuitionistic Fuzzy Sets and Generalized Nets (IWIFSGN-2009) has been meant to commence a new series of scientific events primarily focused on new developments in foundations and applications of intuitionistic fuzzy sets and generalized nets pioneered by Professor Krassimir T. Atanassov. Moreover, other topics related to broadly perceived representation and processing of uncertain and imprecise information and intelligent systems are discussed.

We hope that a collection of main contributions presented at the Workshop, completed with many papers by leading experts who have not been able to participate, will provide a source of much needed information on recent trends in the topics considered.

