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**Negotiation strategies  
of programmable agents in  
Continuous Double Auctions**

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POLISH ACADEMY OF SCIENCES

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# Contents

<b>1</b>	<b>Introduction</b>	<b>5</b>
<b>2</b>	<b>State of art</b>	<b>7</b>
<b>3</b>	<b>Negotiations</b>	<b>9</b>
3.1	Negotiation . . . . .	9
3.2	Bilateral negotiations . . . . .	10
3.3	Auctions . . . . .	10
<b>4</b>	<b>Continuous double auction</b>	<b>13</b>
<b>5</b>	<b>Model of the market</b>	<b>15</b>
5.1	Market mechanism . . . . .	15
5.2	Model . . . . .	16
<b>6</b>	<b>Strategies using only current information</b>	<b>19</b>
6.1	Information Knowledge Behavioral Model . . . . .	19
6.2	Truth-Telling (TT) strategy . . . . .	20
6.3	Pure Simple (PS) strategy . . . . .	20
6.4	Kaplan strategy . . . . .	20
6.5	ZI strategies . . . . .	21
6.5.1	Zero intelligence (ZI) strategy . . . . .	21
6.5.2	Zero intelligence plus (ZIP) strategy . . . . .	21
6.6	Preist and van Tol strategy . . . . .	23
<b>7</b>	<b>GD strategies</b>	<b>25</b>
7.1	Belief functions . . . . .	25
7.2	Price formation . . . . .	27

<b>8</b>	<b>AA strategies</b>	<b>29</b>
8.1	Preliminaries . . . . .	29
8.2	Trader . . . . .	29
8.3	Target price . . . . .	30
8.4	Degree of aggressiveness . . . . .	31
8.5	Volatility parameter . . . . .	33
8.6	Price formation . . . . .	34
<b>9</b>	<b>The FL-strategy</b>	<b>37</b>
9.1	Preliminaries . . . . .	37
9.2	The decision sets . . . . .	37
9.3	Strategy rules for the crisp values . . . . .	38
9.3.1	Logic rules . . . . .	38
9.3.2	Final decision . . . . .	40
9.4	Strategy rules for the fuzzy values . . . . .	41
9.4.1	Preliminaries . . . . .	41
9.4.2	Fuzzy logic rules . . . . .	43
9.4.3	Conclusions of rules . . . . .	45
9.4.4	Final decision . . . . .	46
9.5	Adaptive agents . . . . .	47
9.5.1	Attitude towards risk . . . . .	47
9.5.2	Learning . . . . .	49
	Appendix. Fuzzy sets and fuzzy numbers . . . . .	50
<b>10</b>	<b>Architecture of the multi-agent system</b>	<b>55</b>
10.1	Multi-agent systems . . . . .	55
10.2	Agents participating in the market . . . . .	56
10.3	Data . . . . .	57
10.4	Architecture . . . . .	58
10.5	Communication . . . . .	59
<b>11</b>	<b>Results</b>	<b>61</b>
<b>12</b>	<b>Conclusions</b>	<b>65</b>

# Chapter 1

## Introduction

Auctions as a method of selling and buying goods have a long history, initially there were only ascending auctions with simple rules (now known as English auctions) but with time a variety of types of auctions has emerged. Now, auctions have become a very popular method of trading popularized by on-line auctions as Ebay or Allegro (a big Polish auction platform).

According to definition made by McAfee and McMillan in 1987: "an auction is a market institution with an explicit set of rules determining resource allocation and prices on the basis of bids from the market participants".

A special type of auctions, maybe not the most popular in an on-line internet auctions but interesting from point of view of computer simulation, are so called *double auctions*. In double auctions, there are multiple buyers and sellers on the market that place their offer simultaneously.

In this work we review strategies of agents participating in a double auction. There are a lot of different categories of strategies: some consider history, others are reacting on the last placed bid or apply learning algorithms. Some strategies, as ZI, GD, and AA, have been already reviewed in an earlier publication of the present authors [21]. They are repeated here to make a possibly full compendium of strategies proposed in the literature.

The practical context of this research is the double auction for trading emissions of pollutants. Emission, in this context, is the short name for "permission to emit a unit of greenhouse gas"; its unit is either one tonne of carbon dioxide or the mass of another greenhouse gas which is recalculated to so-called carbon dioxide equivalent (tCO<sub>2e</sub>) emissions. This is expressed in units like Certified Emission Reductions (CERs) or carbon credits. This concept was introduced in the Kyoto Protocol, which entered into force in

16 February 2005, obliging countries that ratified it to limit their greenhouse gases (GHG) emissions below the levels of 1990.

The protocol introduced so called "flexible" market-based mechanisms (Emission Trading, Joint Implementation and Clean Development), which are meant to achieve the common reduction target with minimal costs, without knowledge of the parties cost functions. The emission trading market is still not mature and it is still under the process of adjusting the rules and protocols to make it efficient and resistant to collapsing. The Chicago Climate Exchange market ceased operations in 2010 because the legislation was refused by the US Senate and companies were no longer interested in trading this commodity.

There are different schemes developed for this type of market. In report [26], the English auction trading scheme for emission permit trading was considered. In the present work the double auction mechanism for emission trading is defined, as it is a very popular method of creating efficient markets.

This work summarizes the most well known strategies, that present the evolution of automated negotiation strategies: from simple and intuitive approaches as ZI, PS and ZIP, to more forecasting like GD and adapting as AA strategy. None of the general issues of on-line auctions are discussed here. An interested reader is referred to recent reviews of these matters [12, 17, 24].

The structure of the paper is as follows. In chapter 2 the current state of research on the Continuous Double Auction, emission trading and agent strategies are shortly reviewed. In the following chapter the concept of negotiations and different ways of trading is described. In chapter 4 some informations on double auction are presented. Chapter 5 discusses the formal model of the auction double market used in this paper. The following chapters contain the description of the existing strategies for participants in the continuous double auction, they are divided to strategies using only current information, GD strategies, AA strategies and FL-strategy, that uses fuzzy rules to determine the value of next shout. The general architecture of the implemented software is located in the chapter 10, followed by description of its implementation. In chapter 11 some preliminary results are presented. Conclusions summarizes the whole report. Also future works are sketched there.



## Chapter 2

### State of art

This paper joins the topics of emission trading, market architectures and agent strategies. All of these elements are popular research subjects. A comprehensive description of all existing and historical markets can be found in [15]. In [13] details of auctions (like e.g. one- and two-sided, single- and multi-round, single- and multi-unit, information revealing, first and second price, closing rules) are given. General issues of on-line auctions are discussed in [12, 17, 24].

There is a large number of publications and models of greenhouse gases emission permits trading markets. Economic and ethical consequences of commodification of emissions is thoroughly discussed in [30]. An iterative scheme developed by a group of International Institute for Applied Systems Analysis (IIASA) researchers ([5, 6, 7]) reaches the optimal solution without revealing the cost functions of the parties, but does not consider prices of permits. This procedure assumes a number of iteration where two parties negotiate bilaterally an amount of traded permits until the optimal solution is found.

Klaassen [16] persuades that even in theoretically good market schemes there is a number of factors that prevent reaching the optimal profit in emission trading, as for example imperfect information, speculative behavior and abusing market power.

Researchers from the Systems Research Institute of Polish Academy of Sciences and the IIASA [6, 7, 19, 20] introduced the emission permits trading, in which the uncertainties of emission inventories are taken into account. In [10] authors developed a schema with additional possibility for a party – decreasing the uncertainty by investing in monitoring.

The multi-agent approaches to the problem were published in [22] and [18]. An approach described in [22] is modeling bilateral trades between agents to find the optimal bilateral solution. The core of approach described in [18] is finding optimal price having given offers of demand and supply. A genetic algorithm approach is presented in [31, 32] and is one of few schemes, in which the prices in emission permits trading are considered, not the search for equilibrium price.

# Chapter 12

## Conclusions

Emission permits are a new commodity that can have a very uncertain volume. Moreover, uncertainties for different types of greenhouse gases differ considerably. For example, uncertainty of emission of  $\text{CO}_2$  from a power plant may be few percents, while that of  $\text{N}_2\text{O}$  from agricultural activities may be close to 100%. Thus, a risk for traders to really reach the imposed emission level is much different when buying one or another emissions. Trading under such conditions requires new rules, but also provides a unique base to develop new strategies that are able to fulfill the requirements. Before it will be possible to include uncertainties in the agents behavior, the market scheme has to be designed and tested.

Given the tool as the *multi-agent system*, it is possible to design a market that is simple, dynamic and that allows participants to adjust their desired profit and the time of placing an offer. The continuous double auction chosen in the report has simple rules and does not impose limitations on neither the number of participants nor their strategies.

The aim of the present report is to go through the most well-known strategies for this type of market, to classify them and to summarize their properties. The existing strategies can be divided into few groups: simple and reactive strategies (e.g. TT, ZI, ZIP); strategies that are using historical data to predict the prices (e.g. GD) and strategies that are exploiting features of agents and market configuration (e.g. Kaplan, AA). Most of the strategies (except for the very simple ones) result in the market price converging to equilibrium price and generally in most participants reaching profit.

The next step is to create agents that will dynamically adjust or even change their strategies depending on the situation on the market. After

that, specific features of the emission market will be added to check how agents behave. Limit price will become a function of traded permits and participants would have to consider the level of uncertainty of the traded permit.

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the 1990s, the number of people in the world who are illiterate has increased from 1.1 billion to 1.2 billion (UNESCO, 2003).

There are many reasons for the increase in illiteracy. One of the reasons is that the population growth rate is higher than the literacy rate. Another reason is that the quality of education is low. In many developing countries, the quality of education is so low that it does not help people to become literate. In addition, many people do not have access to education. In many rural areas, there are no schools or the schools are far away from the village. This makes it difficult for people to go to school. Finally, many people do not have the resources to pay for education. This is especially true for women, who often have to take care of their families and do not have time to go to school.

There are many ways to reduce illiteracy. One way is to improve the quality of education. This can be done by training teachers and providing them with the resources they need. Another way is to provide more access to education. This can be done by building schools in rural areas and providing transportation for students. Finally, we can help people pay for education. This can be done by providing scholarships and other financial aid.

Reducing illiteracy is important for many reasons. It helps people to find better jobs and improve their lives. It also helps people to understand their rights and responsibilities. Finally, it helps people to participate in their communities and make a difference in the world.

There are many organizations that are working to reduce illiteracy. One of the most well-known is UNESCO. UNESCO has many programs and projects that help people become literate. Other organizations include the World Bank, the International Labour Organization, and many others.

Reducing illiteracy is a challenge, but it is one that we must face if we want to create a better world for ourselves and for future generations. We must work together to improve the quality of education and provide more access to education. We must also help people pay for education. Only then can we hope to reduce illiteracy and create a world where everyone has the opportunity to learn and grow.

There are many ways to measure illiteracy. One way is to count the number of people who cannot read and write. Another way is to measure the quality of education. This can be done by looking at the number of years of schooling and the quality of the curriculum. Finally, we can measure the impact of education on people's lives. This can be done by looking at their income, their health, and their participation in their communities.

There are many challenges to reducing illiteracy. One of the biggest is that many people do not have access to education. In many rural areas, there are no schools or the schools are far away from the village. This makes it difficult for people to go to school. Another challenge is that many people do not have the resources to pay for education. This is especially true for women, who often have to take care of their families and do not have time to go to school.

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Reducing illiteracy is a goal that we should all strive for. It is a goal that will help us create a better world for ourselves and for future generations. We must work together to overcome the challenges and provide everyone with the opportunity to learn and grow.

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