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MATHEMATICAL PAPERS

OF

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THE COLLECTED

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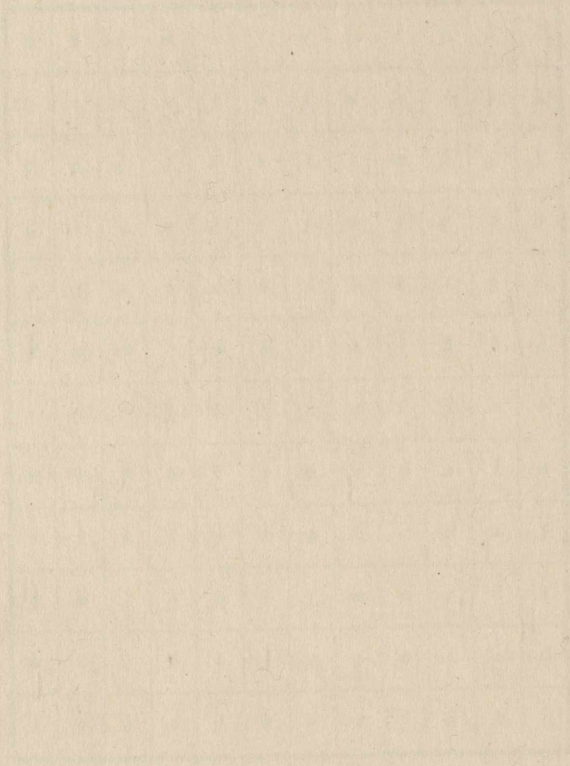
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