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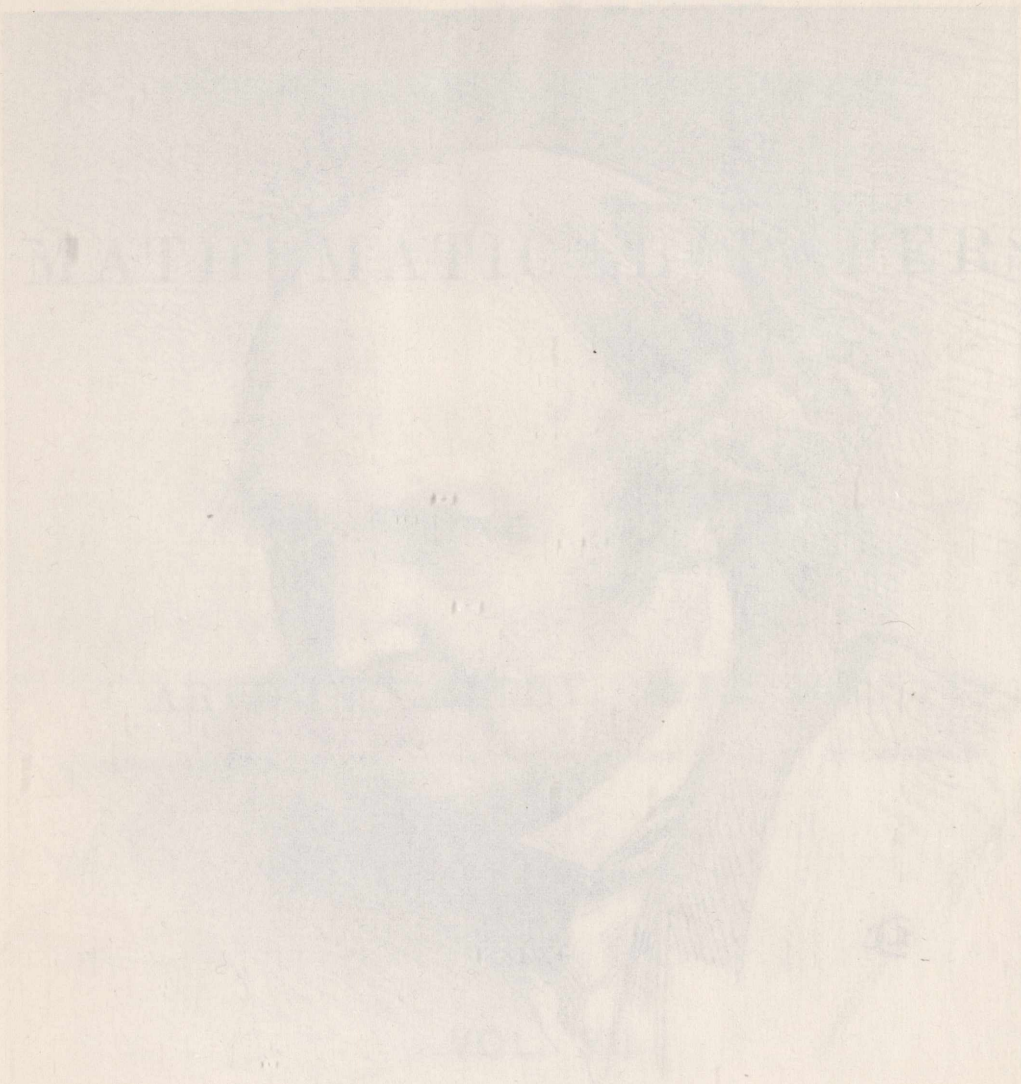

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VOL. VII.

CAMBRIDGE:
AT THE UNIVERSITY PRESS.
1894

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JOHNSON REPRINT CORPORATION
111 Fifth Avenue, New York 3, N.Y.

JOHNSON REPRINT COMPANY LIMITED
Berkeley Square House, London, W. 1.

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opis nr: 47868

INSTYTUT MATEMAT. P.A.N. BIBLIOTEKA
12807/VII

First Reprinting, 1963, Johnson Reprint Corporation

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